

Answer on Question #76609-Physics-Other

In a linear chain of two different types of atoms of masses M and m the displacement of the two atoms in the $k=0$ optical branch are u and v respectively. Show that $u/v = -m/M$

Solution

For a diatomic chain (of two different types of atoms of masses m and M that interact with same force constant C):

$$\frac{u}{v} = \frac{C(1 + e^{-ika})}{2C - M\omega^2}$$

In the $k=0$ optical branch:

$$\omega^2 = 2C \left(\frac{1}{m} + \frac{1}{M} \right)$$

Thus,

$$\frac{u}{v} = \frac{C(1 + e^{-i(0)a})}{2C - M\omega^2} = \frac{C(1 + 1)}{2C - M\omega^2} = \frac{C}{C - \frac{1}{2}M\omega^2}$$

$$\frac{u}{v} = \frac{C}{C - \frac{1}{2}M \cdot 2C \left(\frac{1}{m} + \frac{1}{M} \right)} = \frac{1}{1 - \frac{M}{m} + 1} = -\frac{m}{M}$$

$$\frac{u}{v} = -\frac{m}{M}$$

Answer provided by <https://www.AssignmentExpert.com>