10 If a force of 80N extends a spring of natural length 8m by 0.4m what will be the length of the spring when the applied force is 100N

0.3m

0.5m

1.0m

2.0m

## Solution:

First of all we need to find the spring constant (from Hooke's law):

$$F_1 = k x_1$$

 $F_1$  – applied force in the first case,  $x_1$  – extension.

$$k = \frac{F_1}{x_1} = \frac{80 \text{ N}}{0.4 \text{ m}} = 200 \frac{\text{N}}{\text{m}}$$

So, the length of the spring in the second case will be greater its natural length:

$$x_2 = \frac{F_2}{k} = \frac{100 \text{ N}}{200 \text{ N/m}} = 0.5 \text{ m}$$

And the total length in second case:

$$l = l_0 + x_2 = 8 + 0.5 = 8.5 \text{ m}$$

**Answer:** extension = 0.5 m;

total length when the applied force is 100N =  $8.5\ m$  .

11 A wire of cross-sectional area of  $6 \times 10^{-5}$ m<sup>2</sup> and length 50cm stretches by 0.2mm under a load of 3000N. Calculate the Young's modulus for the wire

8×10<sup>10</sup>Nm<sup>-2</sup> 1.25×10<sup>11</sup>Nm<sup>-2</sup> 2.5×10<sup>11</sup>Nm<sup>-2</sup> 5×10<sup>11</sup>Nm<sup>-2</sup>

## Solution:

Young's modulus E, is

$$E = \frac{F/A}{\Delta L/L}$$

where

E is the Young's modulus (modulus of elasticity)

F is the force exerted on an object under tension;

A is the actual cross-sectional area through which the force is applied;

 $\Delta L$  is the amount by which the length of the object changes;

L is the original length of the object.

Hence,

$$E = \frac{3000/6 \cdot 10^{-5}}{0.2 \cdot 10^{-3}/0.5} = 1.25 \cdot 10^{11} \,\mathrm{Nm^{-2}}$$

**Answer:**  $1.25 \cdot 10^{11} \text{ Nm}^{-2}$