

Answer on Question #41470 – Physics – Other

Question.

If you dive underwater, you notice an uncomfortable pressure on your eardrum due to the increased pressure. The human eardrum has a pressure of 70mm^2 ($7 \cdot 10^{-5} \text{m}^2$) and it can sustain a force of 7N without rupturing. If your body had no means of balancing the extra pressure, what would be the maximum depth you could dive without rupturing the eardrum?

$$S = 70 \text{ mm}^2 = 7 \cdot 10^{-5} \text{ m}^2$$

$$F = 7 \text{ N}$$

$$\rho = 1000 \frac{\text{kg}}{\text{m}^3} // \text{it's the density of water}$$

$$g = 9.8 \frac{\text{N}}{\text{kg}}$$

$$h = ?$$

Solution.

Find the maximum pressure that a person can stand under water:

$$P_{\text{critical}} = \frac{F}{S} = \frac{7}{7 \cdot 10^{-5}} = 10^5 \text{ Pa}$$

Pressure of water column on a person in a depth h is:

$$P_{\text{water}} = \rho gh$$

Pressure at maximum depth h corresponds to the maximum allowable pressure P_{crit} :

$$P_{\text{critical}} = P_{\text{water}}$$

$$\frac{F}{S} = \rho gh$$

So,

$$h = \frac{F}{\rho g S}$$

$$h = \frac{7}{7 \cdot 10^{-5} \cdot 9.8 \cdot 1000} = 10.2 \text{ m}$$

Answer.

$$h = \frac{F}{\rho g S} = 10.2 \text{ m}$$