

Answer to Question #87288 – Math – Calculus

Question

1. Evaluate the limit

$$\lim_{x \rightarrow \infty} \frac{6e^{4x} - e^{-2x}}{8e^{4x} - e^{2x} + 3e^{-x}}$$

Solution

$$\lim_{x \rightarrow \infty} \frac{6e^{4x} - e^{-2x}}{8e^{4x} - e^{2x} + 3e^{-x}} = \lim_{x \rightarrow \infty} \frac{e^{4x}(6 - e^{-6x})}{e^{4x}(8 - e^{-2x} + 3e^{-5x})} = \lim_{x \rightarrow \infty} \frac{(6 - e^{-6x})}{(8 - e^{-2x} + 3e^{-5x})} = \frac{6}{8} = \frac{3}{4}$$

Note: $\lim_{x \rightarrow \infty} e^{-ax} = 0, a > 0$.