

Answer on Question #85653 – Math – Discrete Mathematics

Question

Prove that the conditional proposition and its contrapositive are logically equivalent using the truth table.

Proof

the conditional proposition is $p \rightarrow q$, and its contrapositive is $(\neg q \rightarrow \neg p)$

Truth table:

| p | q | $p \rightarrow q$ | $\neg q \rightarrow \neg p$ |
|---|---|-------------------|-----------------------------|
| T | T | T | T |
| T | F | F | F |
| F | T | T | T |
| F | F | T | T |

Each row of $(\neg q \rightarrow \neg p)$ is identical to the corresponding row of $p \rightarrow q$. Therefore, conditional proposition is logically equivalent to its contrapositive.