

Answer on Question #82646 – Math – Statistics and Probability

Question

Of 535 broiler chickens purchased from various kinds of food stores in different regions of a country and tested for types of bacteria that cause food-borne illnesses, 23% were infected with a particular bacterium.

- a) Construct a 95% confidence interval.
- b) Explain what your confidence interval says about chicken sold in the country.
- c) A government spokesperson claimed that the sample size was too small, relative to the billions of chickens slaughtered each year, to generalize. Is this criticism valid?

Solution

$$\begin{aligned} \text{a) } 95\%CI &= \left(p - z_{0.025} \sqrt{\frac{p(1-p)}{n}}, p + z_{0.025} \sqrt{\frac{p(1-p)}{n}} \right) = \\ &= \left(0.23 - 1.96 \sqrt{\frac{0.23 * 0.77}{535}}, 0.23 + 1.96 \sqrt{\frac{0.23 * 0.77}{535}} \right) = \\ &= (0.1943, 0.2657). \end{aligned}$$

- b) We are 95% confident that the population proportion of the infected broiler chickens lies between 0.1943 and 0.2657.
- c) No. Until the necessary assumptions and conditions for the confidence interval are met, the results can be generalized.