

Answer on Question #80054 – Math – Calculus

Question

$$g(x) = \frac{x - 1}{x^2 - 5x + 6}$$

1. Limit of $g(x)$ as x approaches -2 from left
2. Limit of $g(x)$ as x approaches 3 from right
3. Limit of $g(x)$ as x approaches $-\infty$

Solution

$$g(x) = \frac{x - 1}{x^2 - 5x + 6}$$

1. Limit of $g(x)$ as x approaches -2 from left

$$\lim_{x \rightarrow -2-0} g(x) = \lim_{x \rightarrow -2-0} \frac{x - 1}{x^2 - 5x + 6} = \frac{-3}{20} = -\frac{3}{20}$$

2. Limit of $g(x)$ as x approaches 3 from right

$$\begin{aligned} \lim_{x \rightarrow 3+0} g(x) &= \lim_{x \rightarrow 3+0} \frac{x - 1}{x^2 - 5x + 6} = \lim_{x \rightarrow 3+0} \left(\frac{x - 1}{x - 2} * \frac{1}{x - 3} \right) \\ &= \lim_{x \rightarrow 3+0} \left(\frac{x - 1}{x - 2} \right) * \lim_{x \rightarrow 3+0} \left(\frac{1}{x - 3} \right) = 2 * (+\infty) = +\infty \end{aligned}$$

Here, $x \rightarrow 3+0 \Rightarrow x > 3 \Rightarrow x - 3 > 0$

3. Limit of $g(x)$ as x approaches $-\infty$

$$\begin{aligned} \lim_{x \rightarrow -\infty} g(x) &= \lim_{x \rightarrow -\infty} \frac{x - 1}{x^2 - 5x + 6} \\ &= \lim_{x \rightarrow -\infty} \frac{\frac{1}{x} - \frac{1}{x^2}}{1 - \frac{5}{x} + \frac{6}{x^2}} = \frac{\lim_{x \rightarrow -\infty} \left(\frac{1}{x} - \frac{1}{x^2} \right)}{\lim_{x \rightarrow -\infty} \left(1 - \frac{5}{x} + \frac{6}{x^2} \right)} = \frac{0}{1} = 0 \end{aligned}$$

Answer:

$$g(x) = \frac{x - 1}{x^2 - 5x + 6}$$

1. Limit of $g(x)$ as x approaches -2 from left

$$\lim_{x \rightarrow -2-0} g(x) = -\frac{3}{20}$$

2. Limit of $g(x)$ as x approaches 3 from right

$$\lim_{x \rightarrow 3+0} g(x) = +\infty$$

3. Limit of $g(x)$ as x approaches $-\infty$

$$\lim_{x \rightarrow -\infty} g(x) = 0$$