## Answer on Question #76326 – Math – Discrete Mathematics

## Question

How many ways can you assign 4 caretakers each of which look after 2 lighthouses for a year (for a total of 8 lighthouses), and then assign each two lighthouses in the next year so that none of them tend the same two lighthouses both years?

## Solution

For the first year:

$$N_1 = C_8^2 \cdot C_6^2 \cdot C_4^2 = \frac{8!}{6! \, 2!} \cdot \frac{6!}{4! \, 2!} \cdot \frac{4!}{2! \, 2!} = 28 \cdot 15 \cdot 6 = 2520$$

For the second year:

$$N_2 = (C_8^2 - 1)(C_6^2 - 1)(C_4^2 - 1) = 27 \cdot 14 \cdot 5 = 1890$$

In the second year each caretaker cannot have the same two lighthouses as in the first year, so 1 way (of the first year) for each caretaker is restricted. And we have the given formula for  $N_2$ . In total there will be  $N_1N_2$  ways.