

Answer on Question #69155 – Math – Statistics and Probability

Question

It is noted that 8% of Kaplan students are left handed if 20 (TWENTY) students are randomly selected, calculate the following:

- 1) probability that none of them are left-handed;
- 2) probability that at most 2 are left handed;
- 3) standard deviation for the number of left-handed student;
- 4) if 50 classes of 20 students are randomly selected, what is the probability that 10 classes have no left handed students?

Solution

$$1) P(X = 0) = C_{20}^0 \cdot 0.08^0 \cdot 0.92^{20} = 0.92^{20} \approx 0.1887.$$

$$2) P(X \leq 2) = P(X = 0) + P(X = 1) + P(X = 2) = C_{20}^0 \cdot 0.08^0 \cdot 0.92^{20} + C_{20}^1 \cdot 0.08^1 \cdot 0.92^{19} + C_{20}^2 \cdot 0.08^2 \cdot 0.92^{18} = 0.7879.$$

$$3) \sigma = \sqrt{np(1-p)} = \sqrt{20 \cdot 0.08 \cdot 0.92} \approx 1.2133.$$

4)

$$P(\text{no one in a class is left - handed}) = 0.92^{20} = 0.1887;$$

$$P(\text{at least one in a class is left - handed}) = 1 - 0.1887 = 0.8113;$$

$$P(10 \text{ classes have no left - handed students}) = C_{50}^{10} \cdot 0.1887^{10} \cdot 0.8113^{40} = 0.1370.$$

Answer: 1) 0.1887; 2) 0.7879; 3) 1.2133; 4) 0.1370.