

Answer on Question #67012, Math / Statistics and Probability.

We will use the formula

$$P(A \cap B) = P(A)P(B | A).$$

A is the events such that the first drawing will give 3 black balls.

B is the events such that the second drawing will give 3 blue balls.

$$\text{Then } P(A) = \frac{\binom{3}{5}}{\binom{3}{13}} = \frac{\frac{5!}{3!2!}}{\frac{13!}{3!10!}} = \frac{5!10!}{2!13!} = \frac{3 \cdot 4 \cdot 5}{11 \cdot 12 \cdot 13} = \frac{5}{11 \cdot 13},$$

$$P(B | A) = \frac{\binom{3}{8}}{\binom{3}{10}} = \frac{\frac{8!}{3!5!}}{\frac{10!}{3!7!}} = \frac{8!7!}{5!10!} = \frac{6 \cdot 7}{9 \cdot 10} = \frac{7}{3 \cdot 5}.$$

Therefore

$$P(A \cap B) = P(A)P(B | A) = \frac{5}{11 \cdot 13} \cdot \frac{7}{3 \cdot 5} = \frac{7}{3 \cdot 11 \cdot 13} = \frac{7}{429} = 0.01632.$$

Hence the probability that the first drawing will give 3 black balls and the second 3 blue balls is 0.0163.