Answer on Question #64113 – Math – Calculus

Question

Suppose *f* is an odd function which is differentiable everywhere and *a* is a positive number. Show that for every *a* there exists *c* belong (-a, a) such that f'(c) = f(a)/a

Solution

Since f is odd,

$$f(-a) = -f(a).$$

Since f is differentiable everywhere, the Mean Value Theorem says that there exists c between -a and a such that

$$f'(c) = \frac{f(a) - f(-a)}{a - (-a)} = \frac{2f(a)}{2a} = \frac{f(a)}{a}$$