Answer on Question #63933 - Math - Calculus

Question

1. A particle moves along a straight line according to the law:

 $S = 132 + 10t - 6t^2 + 3t^3.$

Find the following:

- a) The velocity and acceleration at any time t?
- **b)** Velocity at t = 2;
- c) Acceleration at t = 3.

Solution

Let's find laws for velocity and acceleration:

a) Velocity: $V(t) = \frac{dS}{dt} = (132 + 10t - 6t^2 + 3t^3)' = 10 - 12t + 9t^2;$ Acceleration: $A(t) = \frac{dV}{dt} = (10 - 12t + 9t^2)' = -12 + 18t.$

Now we can find velocity and acceleration at any time t:

- **b)** Velocity at t = 2: $V(2) = 10 - 12 \cdot 2 + 9 \cdot 2^2 = 10 - 24 + 36 = 22.$
- c) Acceleration at t = 3: $A(3) = -12 + 18 \cdot 3 = -12 + 54 = 42.$

Answer:

- a) $V(t) = 10 12t + 9t^2$, A(t) = -12 + 18t;
- **b)** V(2) = 22;
- c) A(3) = 42.