Answer on Question #62757 - Math - Statistics and Probability

Question

The data of an experiment to supply sufficient quantities of fertilizer to optimize vegetation growth (grass yield) and avoid excessive application that could lead to a runoff and nutrient enrichment of a nearby lake is shown in the data below. Determine the regression of y on x.

у	25	50	75	100	125	150	175	200	225	250
x	84	9	90	154	148	169	206	244	212	248

Solution

We shall derive the linear regression equation, i.e. we must calculate the coefficients a and b in the equation y = a + bx. Now we calculate the next values:

$$\bar{x} = \frac{84+9+90+154+148+169+206+244+212+248}{10} = 156.4;$$

$$\bar{y} = \frac{25+50+75+100+125+150+175+200+225+250}{10} = 137.5;$$

$$\bar{x}\bar{y} = \frac{84\cdot25+9\cdot50+90\cdot75+154\cdot100+148\cdot125+169\cdot150+206\cdot175+244\cdot200+212\cdot225+248\cdot250}{10} = 26310;$$

$$\sigma_x^2 = \frac{(84-156\cdot4)^2+(9-156\cdot4)^2+(90-156\cdot4)^2+(154-156\cdot4)^2+(148-156\cdot4)^2+(169-156\cdot4)^2+(206-156\cdot4)^2+(244-156\cdot4)^2+(212-156\cdot4)^2+(248-156\cdot4)^2}{10} = 5322.84.$$

Now we can obtain the coefficients using the next formulas:

$$b = \frac{\bar{x}\bar{y} - \bar{x}\cdot\bar{y}}{\sigma_x^2} = 0.90; \ a = \bar{y} - b\bar{x} = -3.68.$$

The regression equation for the given data is $y = -3.68 + 0.90 \cdot x$.

Answer: $y = -3.68 + 0.90 \cdot x$.