

Answer on Question #61965 – Math – Calculus

Question

6 Find the integral with respect to x

$$\int \cos x \sin x dx$$

Solution

$$\int \cos x \sin x dx = \int \sin x d(\sin x) = \frac{(\sin x)^2}{2} + c$$

Answer: $\frac{(\sin x)^2}{2} + c.$

Question

7 Evaluate

$$\int_{-1}^2 (y^2 + y - 2) dy$$

Solution

$$\int_{-1}^2 (y^2 + y - 2) dy = \left(\frac{y^3}{3} + \frac{y^2}{2} - 2y \right)_{-1}^2 = \left(\frac{2^3}{3} + \frac{2^2}{2} - 2(2) \right) - \left(\frac{(-1)^3}{3} + \frac{(-1)^2}{2} - 2(-1) \right) = -\frac{3}{2}$$

Answer: $-\frac{3}{2}.$

Question

8 Integrate with respect to x:

$$\int_{-1}^2 x^2 (x^3 + 4)^2 dx$$

Solution

$$\begin{aligned} \int_{-1}^2 x^2 (x^3 + 4)^2 dx &= \frac{1}{3} \int_{-1}^2 (x^3 + 4)^2 d(x^3 + 4) = \frac{1}{3} \left(\frac{(x^3 + 4)^3}{3} \right)_{-1}^2 = \frac{1}{9} ((2^3 + 4)^3 - ((-1)^3 + 4)^3) \\ &= 189 \end{aligned}$$

Answer: 189.

Question

9 Integrate with respect to x:

$$\int_{-1}^3 \frac{x}{7+x^2} dx$$

Solution

$$\int_{-1}^3 \frac{x}{7+x^2} dx = \frac{1}{2} \int_{-1}^3 \frac{1}{7+x^2} d(x^2 + 7) = \frac{1}{2} \ln(x^2 + 7) \Big|_{-1}^3 = \frac{1}{2} \ln \left(\frac{3^2 + 7}{(-1)^2 + 7} \right) = \frac{1}{2} \ln 2.$$

Answer: $\frac{1}{2} \ln 2$.

Question

10. Integrate with respect to x:

$$\int_1^4 \left(x + \frac{1}{\sqrt{x}} \right) dx$$

Solution

$$\begin{aligned} \int_1^4 \left(x + \frac{1}{\sqrt{x}} \right) dx &= \int_1^4 x dx + \int_1^4 \frac{1}{\sqrt{x}} dx = \frac{x^2}{2} \Big|_1^4 + \frac{x^{-\frac{1}{2}+1}}{-\frac{1}{2}+1} \Big|_1^4 = \frac{x^2}{2} \Big|_1^4 + 2\sqrt{x} \Big|_1^4 = \frac{4^2}{2} - \frac{1^2}{2} + 2\sqrt{4} - 2\sqrt{1} = \\ &= 8 - \frac{1}{2} + 2 \cdot 2 - 2 = 8 - \frac{1}{2} + 4 - 2 = 9.5. \end{aligned}$$

Answer: 9.5.