

Answer on Question #61960 – Math – Calculus

Question

1. Evaluate $\int e^{4x} dx$.

14e4x+c

e^x+c

3e^x+c

13e^x+c

Solution

Using the substitution method we obtain

$$\int e^{4x} dx = \left\{ \begin{array}{l} 4x = y, x = \frac{y}{4} \\ dx = \frac{1}{4} dy \end{array} \right\} = \int \frac{e^y}{4} dy = \frac{e^y}{4} + c = \frac{e^{4x}}{4} + c,$$

where c is an integration constant.

Answer: $\frac{e^{4x}}{4} + c$.

Question

2. Evaluate $\int xe^{6x} dx$.

x6e6x-1136e6x+c

x3e6x+116e6x+c

x6e6x+1136e6x+c

-x6e6x+1136e6x+c

Solution

Using integration by parts we get

$$\int xe^{6x} dx = \left\{ \begin{array}{l} u = x, du = dx \\ dv = e^{6x} dx, v = \frac{e^{6x}}{6} \end{array} \right\} = \frac{x}{6} e^{6x} - \int \frac{e^{6x}}{6} dx = \frac{x}{6} e^{6x} - \frac{e^{6x}}{36} + c,$$

where c is an integration constant.

Answer: $\frac{x}{6} e^{6x} - \frac{e^{6x}}{36} + c$.

Question

3. Find $\int x \cos(ax^2) dx$ with respect to x

$\cos 3x+c$

$\sin 2x+c$

$\sec 2x+1$

$12a \sin ax^2+c$

Solution

If $a \neq 0$, then using the substitution method we obtain

$$\begin{aligned}\int x \cos(ax^2) dx &= \frac{1}{2a} \int 2ax \cos(ax^2) dx = \frac{1}{2a} \int \cos(ax^2) d(ax^2) = \{ax^2 = y\} = \\ &= \frac{1}{2a} \int \cos y dy = \frac{\sin y}{2a} + c = \frac{\sin(ax^2)}{2a} + c,\end{aligned}$$

where $a \neq 0$; c is an integration constant.

If $a = 0$, then $\cos(ax^2) = \cos(0) = 1$ and

$$\int x \cos(ax^2) dx = \int x dx = \frac{x^2}{2} + c,$$

where $a = 0$; c is an integration constant.

Answer: $\frac{\sin(ax^2)}{2a} + c, a \neq 0.$