

Answer on Question #61711 – Math – Algebra

Question

A welder must construct a beam with a total length of $32\frac{7}{8}$ in. If he has already joined a $14\frac{1}{6}$ in beam with a $10\frac{3}{4}$ in beam, find the length of a third beam needed to reach the total length.

Solution

$$\begin{aligned} 32\frac{7}{8} - \left(14\frac{1}{6} + 10\frac{3}{4}\right) &= \frac{32 \cdot 8 + 7}{8} - \left(\frac{14 \cdot 6 + 1}{6} + \frac{10 \cdot 4 + 3}{4}\right) = \\ &= \frac{256 + 7}{8} - \left(\frac{84 + 1}{6} + \frac{40 + 3}{4}\right) = \frac{263}{8} - \left(\frac{85}{6} + \frac{43}{4}\right) \\ &= \text{[the least common multiplier of 8, 6, 4 is 24]} = \\ &= \frac{263 \cdot 3}{8 \cdot 3} - \left(\frac{85 \cdot 4}{6 \cdot 4} + \frac{43 \cdot 6}{4 \cdot 6}\right) = \frac{789}{24} - \left(\frac{340}{24} + \frac{258}{24}\right) = \frac{789}{24} - \frac{598}{24} = \frac{789 - 598}{24} = \\ &= \frac{191}{24} = \frac{168 + 23}{24} = \frac{168}{24} + \frac{23}{24} = 7 + \frac{23}{24} = 7\frac{23}{24} \text{ (in.)} \end{aligned}$$

Answer: $7\frac{23}{24}$ in.