Answer on Question #59020 - Math - Statistics and Probability

Question

3. Each of 12 refrigerators of a certain type has been returned to a distributor because of an audible, highpitched, oscillating noise when the refrigerator is running. Suppose that 7 of these refrigerators have defective compressor and the other 5 have less serious problems. If the refrigerators are examined in random order. Let X be the number among the first 6 examined that have a defective compressor. What is the probability that X exceeds its mean value by more than 1 standard deviation?

Solution

It is hypergeometric probability distribution with N = 12, n = 6, M = 7, N - M = 5.

$$\mu = n\frac{M}{N} = 6\frac{7}{12} = 3.5$$
$$\sigma = \sqrt{n\frac{M}{N}\frac{N-M}{N}\frac{N-n}{N-1}} = \sqrt{6\frac{7}{12}\frac{5}{12}\frac{12-6}{12-1}} = 0.89$$
$$\mu + \sigma = 3.5 + 0.89 = 4.39$$

The probability that X exceeds its mean value by more than 1 standard deviation is

$$P(X > \mu + \sigma) = 1 - P(X < \mu + \sigma) = 1 - F(\mu + \sigma).$$

We used Excel function HYPGEOM.DIST:

F(4.39) = HYPGEOM. DIST(4.39,6,7,12, TRUE) = 0.8788.

 $P(X > \mu + \sigma) = 1 - 0.8788 = 0.1212.$

Answer: 0.1212.

Question

4. The error involved in making a certain measurement is a continuous rv X with pdf

f(x)={0.09375(4-x 2)0 -2≤x≤20therwise

$$f(x) = \begin{cases} 0.09375(4 - x^2), -2 \le x \le 2\\ 0, & otherwise \end{cases}$$

compute P(-1<x<1)

Solution

$$P(-1 < x < 1) = \int_{-1}^{1} 0.09375(4 - x^{2}) = 0.09375\left(4x - \frac{x^{3}}{3}\right)_{-1}^{1} = 0.09375\left(8 - \frac{2}{3}\right) = 0.6875.$$

Answer: 0.6875.

www.AssignmentExpert.com