Answer on Question #58283 – Math – Complex Analysis

The polar form of the complex number

$$z = x + iy$$

is given by

Solution:

The polar form of the complex number **z** is

$$z = r(\cos\varphi + i\sin\varphi)$$

where

 $r = |z| = \sqrt{x^2 + y^2}$ is the absolute value of the complex number z

and

 φ =arg(z) is the argument of the complex number z:

$$\varphi = \arg(x + iy) = \begin{cases} \arctan\left(\frac{y}{x}\right) & \text{if } x > 0\\ \pi + \arctan\left(\frac{y}{x}\right) & \text{if } x < 0 \text{ and } y \ge 0\\ -\pi + \arctan\left(\frac{y}{x}\right) & \text{if } x < 0 \text{ and } y < 0\\ \frac{\pi}{2} & \text{if } x = 0 \text{ and } y < 0\\ -\frac{\pi}{2} & \text{if } x = 0 \text{ and } y < 0\\ \text{indeterminate} & \text{if } x = 0 \text{ and } y = 0 \end{cases}$$

Answer: $z = \sqrt{x^2 + y^2} (\cos[\arg(x + iy)] + i \sin[\arg(x + iy)])$