Answer on Question \# 57225 - Mathematic - Calculus

## Question:

What is the length of the conjugate axis?

$$
\begin{equation*}
\frac{(x-2)^{2}}{36}-\frac{(y+1)^{2}}{64}=1 \tag{1}
\end{equation*}
$$

## Solution:

The equation (1) describes the hyperbola with horizontal transverse axis. In general case its canonical equation has the form

$$
\begin{equation*}
\frac{(x-h)^{2}}{a^{2}}-\frac{(y-k)^{2}}{b^{2}}=1 \tag{2}
\end{equation*}
$$

where ( $h, k$ ) are the coordinates of the center (fig.1).
Definition: if two points $B$ and $B^{\prime}$ are on the $y$-axis such that $C B=C B^{\prime}=b$, then the line segment $B B^{\prime}$ is called the conjugate axis of the hyperbola. Therefore, the length of conjugate axis is $2 b$.


Fig. 1
Let’s rewrite (1) as

$$
\begin{equation*}
\frac{(x-2)^{2}}{6^{2}}-\frac{(y+1)^{2}}{8^{2}}=1 . \tag{3}
\end{equation*}
$$

As we see, the point $C(2,-1)$ is the center of hyperbola (3) (fig.2), and $b=8$.


Fig. 2

Therefore, the length of conjugate axis is equal $2 b=2 \cdot 8=16$ units.
Answer: the length of conjugate axis is 16 units.

