

Answer on Question #57016 - Math - Algebra

Question

1. Which of the following are true statements?

Check all that apply

$$\log(M/N) = \log M - \log N$$

$$\log M^p = p \cdot \log M$$

$$(\log M)^p = p \cdot \log M$$

$$\log(M/N) = \log M / \log N$$

Solution

$$\log(M/N) = \log M - \log N$$

$$\log M^p = p \cdot \log M$$

are true, the rest are false.

Question

2. Fill in the blank: $\log_{\text{sub } 5} 625 = \underline{\hspace{2cm}} \cdot \underline{\hspace{2cm}}$

Solution

$$\log_{\text{sub } 5} 625 = 4$$

$$\log_{\text{sub } 5} 625 = x \Rightarrow$$

$$5^x = 625 \Rightarrow$$

$$5^x = 5^4 \Rightarrow$$

$$x = 4$$

Answer: 4.

Question

3. Which of the following equations is equivalent to $b^v = x$?

A: $y = \ln x$

B: $y = \log_b X$

C: $y = \log_b Y$

D: $y = \log X$

Solution

There is a mistake in statement of this question, $b^v = x$ – instead of “v” should be “y”)

B: $y = \log_b X$

Question

4. Rewrite the following expression as a single logarithm:

$$(2\log(x + 3) + 2\log(x - 2)) - (3\log(x - 7) + \log(x^2))$$

$$\frac{(x+3)^2 (x-7)^3}{(x-2)^{-5} x^{-2}}$$

A: \log (-----)

$$\frac{(x+3)^2 (x-2)^2}{(x-7)^3 x^2}$$

B: \log (-----)

$$\frac{(x+3)^2 (x-7)^3}{x^2 (x-2)^5}$$

C: \log (-----)

$$\frac{x^2 (x+3)^2 (x-7)^3}{x^2 (x-2)^5}$$

D: \log (-----)

Solution

$$\begin{aligned} & (2\log(x+3) + 2\log(x-2)) - (3\log(x-7) + \log(x^2)) \\ &= \log((x+3)^2(x-2)^2) - \log((x-7)^3x^2) = \log \frac{(x+3)^2(x-2)^2}{(x-7)^3x^2} \end{aligned}$$

Answer:

$$(x+3)^2 (x-2)^2$$

$$\frac{(x+3)^2 (x-2)^2}{(x-7)^3 x^2}$$

Question

5. If $\log x = -5$, what is x ?

- A: 0.00001
- B: -0.00001
- C: -0.00005
- D: 0.00005

Solution:

A: 0.00001

$$\log x = -5 \Rightarrow 10^{-5} = x \Rightarrow x = 1/100000 \Rightarrow x = 0.00001.$$