Problem.

Determine the range of values of $\theta \in [0, 2\pi]$ for which the point (cos θ , sin θ) lies inside the triangle formed by the lines x + y = 2; x - y = 1 & 6x + 2y - 10 = 0.

Answer.

These lines don't form a triangle.

Solution.

Let's determine the coordinates of the points of intersection of the lines given.

 $\begin{cases} x + y = 2, \\ x - y = 1; \end{cases} \begin{cases} 2x = 3, \\ 2y = 1; \end{cases} \begin{cases} x = 1.5, \\ y = 0.5. \end{cases} (1.5, 0.5).$ $\begin{cases} x + y = 2, \\ 6x + 2y - 10 = 0; \end{cases} \begin{cases} x + y = 2, \\ 3x + y = 5; \end{cases} \begin{cases} 2x = 3, \\ x + y = 2; \end{cases} \begin{cases} x = 1.5, \\ y = 0.5. \end{cases} (1.5, 0.5).$ $\begin{cases} x - y = 1, \\ 6x + 2y - 10 = 0; \end{cases} \begin{cases} x - y = 1, \\ 3x + y = 5; \end{cases} \begin{cases} 4x = 6, \\ x - y = 1; \end{cases} \begin{cases} x = 1.5, \\ y = 0.5. \end{cases} (1.5, 0.5).$

So, the three lines are concurrent, thus don't form the triangle.

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