

Answer on Question #56037 – Math – Analytic Geometry

Evaluate $(2\mathbf{i} - 4\mathbf{k}) \times (\mathbf{i} + 2\mathbf{j})$.

- a) $8\mathbf{i} - 4\mathbf{j} + 4\mathbf{k}$
- b) $2\mathbf{i} + 4\mathbf{j} + 3\mathbf{k}$
- c) $3\mathbf{i} + 4\mathbf{j} + 2\mathbf{k}$
- d) $5\mathbf{i} - 3\mathbf{j} - \mathbf{k}$

Solution

The cross (vector) product can be rewritten in the following form:

$$\begin{aligned}(2\mathbf{i} - 4\mathbf{k}) \times (\mathbf{i} + 2\mathbf{j}) &= \begin{vmatrix} \mathbf{i} & \mathbf{j} & \mathbf{k} \\ 2 & 0 & -4 \\ 1 & 2 & 0 \end{vmatrix} = \mathbf{i} \begin{vmatrix} 0 & -4 \\ 2 & 0 \end{vmatrix} - \mathbf{j} \begin{vmatrix} 2 & -4 \\ 1 & 0 \end{vmatrix} + \mathbf{k} \begin{vmatrix} 2 & 0 \\ 1 & 2 \end{vmatrix} = \\ &= 8\mathbf{i} - 4\mathbf{j} + 4\mathbf{k}.\end{aligned}$$

Answer: $(2\mathbf{i} - 4\mathbf{k}) \times (\mathbf{i} + 2\mathbf{j}) = 8\mathbf{i} - 4\mathbf{j} + 4\mathbf{k}$.