Answer on Question #55967 - Math - Complex Analysis

Question

Find all z, such that $z^{2015} = 321$.

Solution

Let w=312, then ho=321, $\phi=0$. Then using the formula

$$\sqrt[n]{w} = \left\{ \sqrt[n]{\rho} e^{\frac{\varphi + 2\pi k}{n}i}, k = 0, 1, ..., n - 1 \right\}$$
 we obtain:

$$z = \sqrt[2015]{321 + i \cdot 0} = \left\{ \sqrt[2015]{321} e^{\frac{2\pi k}{2015}i}, k = 0, 1, \dots, 2014 \right\}, \text{ where } \sqrt[2015]{321} \approx 1.003.$$

Answer:
$$\left\{ \sqrt[2015]{321}e^{\frac{2\pi k}{2015}i}, k = 0, 1, ..., 2014 \right\}$$
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