

Answer on Question #55095 – Math – Calculus

suppose $f(x,y) = \sin^2 x \cos y + xy^2$, what is df/dx ?

Solution

$$\frac{df}{dx} = \frac{\partial f}{\partial x} \cdot \frac{dx}{dx} + \frac{\partial f}{\partial y} \cdot \frac{dy}{dx} = \frac{\partial f}{\partial x} + \frac{\partial f}{\partial y} \cdot \frac{dy}{dx}$$

$$\begin{aligned} \frac{\partial f}{\partial x} &= (\sin^2 x \cdot \cos y + x \cdot y^2)'_x = (\sin^2 x)'_x \cdot \cos y + \sin^2 x \cdot (\cos y)'_x + x'_x \cdot y^2 + x \cdot (y^2)'_x = \\ &= 2 \cdot \sin x \cdot \cos x \cdot \cos y + y^2 \end{aligned}$$

$$\begin{aligned} \frac{\partial f}{\partial y} &= (\sin^2 x \cdot \cos y + x \cdot y^2)'_y = (\sin^2 x)'_y \cdot \cos y + \sin^2 x \cdot (\cos y)'_y + x'_y \cdot y^2 + x \cdot (y^2)'_y = \\ &= -\sin^2 x \cdot \sin y + 2xy \end{aligned}$$

$$\begin{aligned} \frac{df}{dx} &= (2 \cdot \sin x \cdot \cos x \cdot \cos y + y^2) - (\sin^2 x \cdot \sin y - 2xy) \frac{dy}{dx} = \sin 2x \cdot \cos y + y^2 - \\ &- \sin^2 x \cdot \sin y \cdot y' + 2xyy' \end{aligned}$$

Answer: $\sin 2x \cdot \cos y + y^2 - \sin^2 x \cdot \sin y \cdot y' + 2xyy'$