Answer on Question #54885 - Math - Statistics and Probability

Most people think that the "normal" adult body temperature is 98.6 degrees. That figure based on 19thcentury study, has recently been challenged. In a 1992 article in the journal of the American medical association, researchers reported that a more accurate figure may be 98.2 degree. Furthermore the standard deviation appeared to be around 0.7 degrees. Assume that a normal model is appropriate.

a) in what interval would you expect most people's body temps to be? Explain

b) what fraction of people would be expected to have body temperatures above 98.6?

c) Below what body temp are the coolest 20% of all people?

Solution

a) 95% of values are within 2 standard deviations of the mean, so

$$98.2 \pm 2 \cdot 0.7 = 96.8 \text{ to } 99.6$$

b)

$$z = \frac{x - \mu}{s} = \frac{98.6 - 98.2}{0.7} = 0.57.$$

Using z-table calculate

$$P(z > 0.57) = 1 - P(z < 0.57) = 1 - 0.7157 = 0.2843.$$

c) The z value for the lowest 20% is

$$z = -0.8416$$
 (*from a table*)

Using the z formula calculate

$$x = \mu + z\sigma = 98.2 - 0.8416 \cdot 0.7 = 97.61.$$