Answer on Question #53276 - Math - Calculus

Question

The *n*th derivative of the function t(x) where $t(x) = 5x^6 - 9x^5 + 3x^3 - 0.5$ is a cubic function.

- (a) State the value of n.
- (**b**) Find the ratio of coefficient in x^3 to the coefficient in x^2 of the cubic function giving your answer in the form 1:k(1 is to k)where k is a fraction in its simplest form.

Solution

(a) Let us take derivatives of t(x) until we get a cubic function.

$$\frac{d}{dx}t(x) = 30x^5 - 45x^4 + 9x^2$$

$$\frac{d^2}{dx^2}t(x) = \frac{d}{dx}\left(\frac{d}{dx}t(x)\right) = 150x^4 - 180x^3 + 18x$$

$$\frac{d^3}{dx^3}t(x) = \frac{d}{dx}\left(\frac{d^2}{dx^2}t(x)\right) = 600x^3 - 540x^2 + 18$$

 $\frac{d^3}{dx^3}t(x)$ is cubic function, thus, 3^{rd} derivative of the function t(x) is a cubic function, hence n=3.

(**b**) The ratio of coefficient in x^3 to the coefficient in x^2 :

$$\frac{600}{-540} = -\frac{60}{54} = -\frac{20}{18} = -\frac{10}{9}$$

Answer:

- (a) 3
- **(b)** $-\frac{10}{9}$