

## Answer on Question #52191 – Math – Calculus

Leibnitz formula is given by

### Solution

**Leibnitz formula for the n-th derivative of a product:**

$$(fg)^{(n)} = \sum_{k=0}^n \binom{n}{k} f^{(n-k)} g^{(k)}, \text{ where } \binom{n}{k} = \frac{n!}{(n-k)!k!}$$

If  $n = 1$  then  $(fg)' = f'g + fg'$ .

**Leibnitz Formula for  $\pi$ :**

$$\frac{\pi}{4} = \sum_{n=1}^{\infty} \frac{(-1)^n}{2n+1}$$

**Leibnitz rule for differentiation under the integral sign:**

$$\frac{d}{dx} \left( \int_{y_0}^{y_1} f(x, y) dy \right) = \int_{y_0}^{y_1} \frac{\partial f(x, y)}{\partial x} dy,$$

where  $y_0$  and  $y_1$  are fixed real numbers

$$\frac{d}{dx} \left( \int_u^v f(x, y) dy \right) = \int_u^v \frac{\partial f(x, y)}{\partial x} dy + f(x, v) \frac{dv}{dx} - f(x, u) \frac{du}{dx},$$

where  $u$  and  $v$  are functions of  $x$ .