

Answer on Question #52180 – Math – Vector Calculus

Question

Let $a = 2i - j$ and $b = i + j + k$, evaluate $a \times b$.

$3k+2j-i$

$i+2j+3k$

$3k-2j-i$

$i+2j-3k$

Solution

If $a = 2i - j$ and $b = i + j + k$, then the cross product $a \times b$ is

$$\begin{aligned} a \times b &= \begin{vmatrix} i & j & k \\ 2 & -1 & 0 \\ 1 & 1 & 1 \end{vmatrix} = i \begin{vmatrix} -1 & 0 \\ 1 & 1 \end{vmatrix} - j \begin{vmatrix} 2 & 0 \\ 1 & 1 \end{vmatrix} + k \begin{vmatrix} 2 & -1 \\ 1 & 1 \end{vmatrix} \\ &= i(-1 * 1 - 1 * 0) - j(2 * 1 - 1 * 0) + k(2 * 1 - 1(-1)) = -i - 2j + 3k. \end{aligned}$$

Answer: $a \times b = 3k - 2j - i$.