

Answer on Question #50620 – Math – Combinatorics | Number Theory

Question

There are 5 students of department A and 5 of department B. How many arrangements are possible around a circular table where 2 students of department B will not sit beside?

I solve this like this.

Students of department B can sit at the middle of 2 students of department A. So there are 5 empty places between the students of department A. So in this 5 place 5 students of department B can sit in $5!$ Ways.

And the students of department A can change their position in $(5-1)! = 4!$ ways.

So in total it is $5! \cdot 4!$ That's it. My question is we know in circular permutation its $(n-1)!$ So i do $(5-1)!$ for department A students. Why it is not done for department B students. They also in a circle. Please explain

Solution

We know in circular permutation there are $(n-1)!$ different arrangements, but at first we should choose A or B department $(n - 1)!$

At second we should count not only circular permutation, but relative position of department A from department B (we have n positions for the first student of department A):

$$n(n - 1)! = n!$$

The total number of different arrangements is $n! (n - 1)!$

Example. When $n = 2$ there is $(2 - 1)! = 1$ arrangement in circular permutation for department A and $(2 - 1)! = 1$ arrangement in circular permutation for department B. Nevertheless, relative position of department A from department B gives 2 arrangements. So,

$$2! (2 - 1)! = 2.$$