Answer on Question #48816 – Math – Complex Analysis

if Ln z = Ln (z*), prove z is real number

Solution

Let complex number be z = a + bi. Then $z^* = a - bi$.

Ln z = ln |z| + i * phi, where phi is angle in complex interpretation of z.

For z^* , Ln $z^* = \ln |z^*| - i^*$ phi.

As we know, $|z| = |z^*|$ and according to statement of question, $Ln z = Ln z^*$.

So, we obtain next equation:

 $\ln |z| + i^{*} phi = \ln |z^{*}| - i^{*} phi.$

It transforms to

I * phi = 0, which means that z is real number.