

Answer on Question #86237 - Chemistry - Physical Chemistry

Question:

How to derive the relation between $\Delta_r U$ and $\Delta_r H$ for a chemical reaction and how is this relation given for the condensed phases and ideal gases?

Solution:

Enthalpy is defined as

$H = U + PV$ where U is internal energy of system and PV are pressure and volume of system

$$H(\text{in}) = U(\text{in}) + PV(\text{in})$$

$$PV = nRT$$

$$H(\text{inl}) = U(\text{in}) + n(\text{in})RT$$

$$H(\text{final}) = U(\text{final}) + PV(\text{final})$$

$$H(\text{final}) = U(\text{final}) + n(\text{final})RT$$

$$D(H) = H(\text{final}) - H(\text{initial})$$

$$D(H) = D(U) + (n(\text{final}) - n(\text{initial}))RT$$

Or we can explain this in more detail in this way, solids and liquids do not show significant changes in volume when heated. So, if volume change, ΔV is insignificant

$$H = U + P\Delta V$$

$$H = U + P(0)$$

$$H = U$$

The difference between the change in internal energy and enthalpy becomes significant when the reaction involves gases.

Consider the chemical reaction that occurs at constant temperature, T and constant pressure, P .

Now, say, the volume of reagents - V_A , and the number of moles in the reagents - n_A . Similarly, the volume of products is V_B , and the number of moles in the product is n_B .

We know that, according to the ideal gas equation,

$$Pv = nRT$$

$$pV_A = n_A RT; pV_B = n_B RT$$

$$pV_B - pV_A = n_B RT - n_A RT$$

$$p(V_B - V_A) = RT(n_B - n_A)$$

$$p\Delta v = Rn_g RT$$

$$H = U + p\Delta v$$

$$H = U + Rn_g RT$$