

For the reaction, $\text{CO(g)} + 2\text{H}_2\text{(g)} = \text{CH}_3\text{OH(g)}$ derive an expression for the equilibrium constant, K_p in terms of the extent of reaction, ϵ and the total pressure p_t , if initially 2 mol of CO and 3 mol of H_2 are mixed.

Solution. The general expression for the equilibrium constant is written as: $K_p = \frac{p_{\text{CH}_3\text{OH}}}{p_{\text{H}_2}^2 \times p_{\text{CO}}}$.

We have a degree of reaction ϵ . Then reacted: 2ϵ moles CO , 4ϵ moles H_2 , and formed: 2ϵ moles CH_3OH . Then the equilibrium quantities of substances:

- for CO : $(2-2\epsilon)$ moles;
- for H_2 : $(3-4\epsilon)$ moles;
- for CH_3OH : 2ϵ moles.

We have a total pressure p_t , then partial pressures:

-for CO : $p_{\text{CO}} = \frac{2-2\epsilon}{2-2\epsilon+3-4\epsilon+2\epsilon} p_t = \frac{2-2\epsilon}{5-4\epsilon} p_t$;

-for H_2 : $p_{\text{H}_2} = \frac{3-4\epsilon}{5-4\epsilon} p_t$;

-for CH_3OH : $p_{\text{CH}_3\text{OH}} = \frac{2\epsilon}{5-4\epsilon} p_t$.

Then the expression of the equilibrium constant takes the form:

$$K_p = \frac{\epsilon(5-4\epsilon)^2}{(1-\epsilon)(3-4\epsilon)^2 p_t^2}$$

Answer: $K_p = \frac{\epsilon(5-4\epsilon)^2}{(1-\epsilon)(3-4\epsilon)^2 p_t^2}$.