

Answer on Question #83277, Chemistry / General Chemistry

The reaction $A(aq) \rightarrow B(aq) + C(aq)$ is a first-order reaction. The half-life of $A(aq)$ is 92.3 s at 25.0°C and its half-life is 70.9 s at 45.0°C. What is its half-life (in s) at 65.0°C?

Solution

For first-order reaction:

$$T_{1/2} = \frac{\ln 2}{k_1}; \text{ where } T_{1/2} \text{ – the half-life, } k_1 \text{ – reaction rate constant upon certain temperature.}$$

Find k_1 and k_2 for the reaction at 25.0°C (298 K) and 45.0°C (318 K)

$$k = \frac{\ln 2}{T_{1/2}} = \frac{0.693}{T_{1/2}};$$

$$k_1 = \frac{0.693}{92.3} = 7.51 \times 10^{-3} \text{ (s}^{-1}\text{)} \text{ – reaction rate constant upon 298 K;}$$

$$k_2 = \frac{0.693}{70.9} = 9.77 \times 10^{-3} \text{ (s}^{-1}\text{)} \text{ – reaction rate constant upon 318 K.}$$

According to Arrhenius equation:

$$k = A \times e^{-\frac{E_a}{RT}}; \text{ where}$$

k – reaction rate constant upon certain temperature;

A – Arrhenius constant or frequency factor;

E_a – activation energy;

R, T – gas constant and temperature.

After logarithmization the equation looks:

$$\ln k = \ln A - \frac{E_a}{RT};$$

Mark $\ln A$ as X and E_a as Y , then

$$\ln k = X - Y/RT$$

$$X = \ln k + Y/RT$$

As X and Y are constants specific for the reaction and temperature independent, find them using the system of equations:

$$X = \ln (7.5 \times 10^{-3}) + \frac{Y}{8.314 \times 298} = -4.89 + \frac{Y}{2477.5}$$

$$X = \ln (9.8 \times 10^{-3}) + \frac{Y}{8.314 \times 318} = -4.63 + \frac{Y}{2643.9}$$

$$-4.89 + \frac{Y}{2477.5} = -4.63 + \frac{Y}{2643.9}$$

$$\frac{Y}{2477.5} - \frac{Y}{2643.9} = -4.63 + 4.89 = 0.26$$

$$2643.9Y - 2477.5Y = 0.26 \times 2643.9 \times 2477.5$$

$$166.4Y = 1703068$$

$$Y = 10\,234.8$$

$$X = -4.89 + \frac{10234.8}{2477.5} = -0.76$$

Find k for the reaction upon 65.0°C (338 K)

$$\ln k = -0.76 - \frac{10234.8}{8.314 \times 338}$$

$$\ln k = -0.76 - 3.64$$

$$\ln k = -4.4$$

$$k = e^{-4.4} = 1.22 \times 10^{-2}$$

Find the half-life of A (aq) at 65.0°C:

$$T_{1/2} = \frac{\ln 2}{k} = \frac{0.693}{0.0122} = \mathbf{56.8 \text{ (s)}}$$

Answer

The half-life of A (aq) is **56.8 s** at 65.0°C