

a) The differential form of the Gibbs energy is:

$$dG = VdP - SdT$$

This differential can be used to determine both the pressure and temperature dependence of the free energy.

G – Gibbs free energy, dG - differential form of the Gibbs free energy, S – entropy, V – volume, T – temperature, P – pressure.

$$b) \Delta G = \Delta H - T\Delta S = -286000\text{J/mol} - 373.15\text{K} \cdot 70\text{J/mol}\cdot\text{K} = -312120.5 \text{ J/mol}$$

$\Delta G < 0$, the process will proceed spontaneously.

$$c) d\ln K_{\text{eq}} = -\frac{\Delta H^0}{R} d(1/T)$$

$$\ln\left(\frac{K_2}{K_1}\right) = -\frac{\Delta H^0}{R} \left(\frac{1}{T_2} - \frac{1}{T_1}\right)$$

From this form of the van't Hoff's equation, we see that at constant pressure, a plot with $\ln K_{\text{eq}}$ on the y-axis and $1/T$ on the x-axis has a slope given by $-\Delta H/R$. For an endothermic reaction, the slope is negative, for an exothermic reaction, the slope is positive.

$$d) \ln(K_2) - \ln(K_1) = \frac{\Delta H^0}{R} \left(\frac{1}{T_1} - \frac{1}{T_2}\right)$$

$$\ln(0.010898) - \ln(0.1678) = \frac{\Delta H^0}{R} \left(\frac{1}{1274} - \frac{1}{1073}\right)$$

$$-4.52 + 1.78 = \frac{\Delta H^0}{R} (0.000785 - 0.000932)$$

$$-2.74 = \frac{\Delta H^0}{R} (-0.000147)$$

$$\frac{\Delta H^0}{R} = 18639.5 \text{ kJ/mol} - \text{the standard molar enthalpy change}$$