A bomb calorimeter, or a constant volume calorimeter, is a device often used to determine the heat of combustion of fuels and the energy content of foods.

In an experiment, a 0.6738 g sample of benzoic acid (C7H6O2) is burned completely in a bomb calorimeter. The calorimeter is surrounded by 1.190×103 g of water. During the combustion the temperature increases from 25.91 to 28.80 °C. The heat capacity of water is 4.184 J g-1°C-1.

The heat capacity of the calorimeter was determined in a previous experiment to be 961.3 $J/^{\circ}C$.

Assuming that no energy is lost to the surroundings, calculate the molar heat of combustion of benzoic acid based on these data.

$$C7H6O2(s) + (15/2) O2(g) 3 H2O(l) + 7 CO2(g) + Energy$$

Solution

We have a reaction of combustion, where heat is released. This heat is absorbed by water in calorimeter and calorimeter itself.

1. Find heat absorbed by water:

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Q_{water} = cm\Delta T;

c = 4.184 \text{ J g-1°C-1};

m(H_2O) = 1.190 \cdot 10^3 \text{ g} = 1190 \text{ g};

\Delta T = T_2 - T_1 = 28.80 - 25.91 = 2.89 \text{ (°C)};

Q_{water} = 4.184 \cdot 1190 \cdot 2.89 = 14389,19 \text{ J}.
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2. Find heat absorbed by calorimeter:

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Q_{cal} = C_{cal} \cdot \Delta T;

C_{cal} = 961.3 \text{ J/°C};

\Delta T = T_2 - T_1 = 28.80 - 25.91 = 2.89 \text{ (°C)};

Q_{cal} = 961.3 \cdot 2.89 = 2778.16 \text{ J}.
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3. Find total heat absorbed by water and calorimeter:

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Q_{surrounding} = Q_{water} + Q_{cal};

Q_{surrounding} = 14389.19 + 2778.16 = 17167.35 (J)
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4. Heat of combustion is the same in magnitude but opposite in sign(heat of combustion is the internal energy that is decreased while the external energy is increased).

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Q_{reaction} = -Q_{surrounding} = -17167.35 J.
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5. Find molar heat of combustion:

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Chemical amount of benzoic acid n(C_7H_6O_2)=m/M; M(C_7H_6O_2)=12.01\cdot7+1.01\cdot6+16.00\cdot2=122.13 (g/mol); n(C_7H_6O_2)=0.6738/122.13=0.00552 (mol). When 0.00552 mol of benzoic acid is burned -- heat of combustion is -17167.35 J, When 1 mole of benzoic acid is burned -- heat of combustion is x J.
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0.00552/1 = -17167.35/x;x= -3110027.17; $\Delta H_{comb} = -3110027.17 \text{ J/mol} = -3110 \text{kJ/mol}$

Answer: -3110kJ/mol