

### Question #70891

A 2.50-kg block of hot iron ( $c_{Fe} = 0.45 \text{ J/g K}$ ;  $T_{in} = 300 \text{ C}$ ) is dropped in cold water ( $T_{in} = 20 \text{ C}$ ) to cool quickly. How much heat needs to be absorbed to cool the iron block to 25 C? How much cold water will be needed? What will happen if 10.0 L of cold water are used?

### Solution

$$1) Q = cm\Delta T$$

Q – heat absorbed or emitted, J;

c – specific heat capacity, J/g K;

m – mass, g;

$\Delta T$  – change of temperature.

$Q = 0.45 \times 2500 \times (300 - 25) = \mathbf{309\ 375 \text{ (J)}}$  – heat needed to be absorbed to cool the iron block to 25 C.

$$2) m = \frac{Q}{c\Delta T}, \quad c(\text{H}_2\text{O}) = 4.2 \text{ J/g K};$$

$m = \frac{309\ 375}{4.2 \times (25 - 20)} = \mathbf{14\ 732 \text{ (g)}}$  or  $\mathbf{14.732 \text{ (kg)}}$  – mass of cold water needed to cool the iron block to 25 C.

3) The heat emitted by iron is equal to the heat absorbed by water and the final temperature of iron cooled and water heated is the same.

$$c_1 m_1 \Delta T = c_2 m_2 \Delta T$$

$$c_1 m_1 (300 - T) = c_2 m_2 (T - 20)$$

$$300 c_1 m_1 - c_1 m_1 T = c_2 m_2 T - 20 c_2 m_2$$

$$300 c_1 m_1 + 20 c_2 m_2 = c_2 m_2 T + c_1 m_1 T$$

$$300 c_1 m_1 + 20 c_2 m_2 = (c_2 m_2 + c_1 m_1) T$$

$$T = \frac{300 c_1 m_1 + 20 c_2 m_2}{c_2 m_2 + c_1 m_1}$$

$T = \frac{300 \times 0.45 \times 2500 + 20 \times 4.2 \times 10000}{4.2 \times 10000 + 0.45 \times 2500} = \frac{337500 + 840000}{42000 + 1125} = \frac{1177500}{43125} = \mathbf{27.3 \text{ (C)}}$  – if 10.0 L of cold water are used, iron block will be cooled to 27,3 C.

### Answer

**309 375 (J)** – heat needed to be absorbed to cool the iron block to 25 C.

**14.732 (kg)** – mass of cold water needed to cool the iron block to 25 C.

Iron block will be cooled to **27,3 C**, if 10.0 L of cold water are used.

Answer provided by <https://www.AssignmentExpert.com>