

Answer on the question #62973, Chemistry / Physical Chemistry

Question:

The equilibrium vapour pressure over a solid at 300K is known to be 20 Torr, and the enthalpy of sublimation is 8.0 kcal mol⁻¹. Determine the equilibrium vapour pressure over the solid at 350K, assuming that ΔH_{subl} is a constant

Solution:

To solve this, we use Clausius-Clapeyron equation.

This equation relates the vapour pressure, enthalpy of sublimation and temperature:

$$\ln(P) = \text{const} - \frac{\Delta H_{\text{subl}}}{RT}$$

Then, vapour pressure change for different temperatures is:

$$\ln\left(\frac{P_2}{P_1}\right) = \frac{\Delta H_{\text{subl}}}{R} \left(\frac{1}{T_1} - \frac{1}{T_2}\right)$$

Then, $T_1 = 300\text{K}$ and $T_2 = 350\text{K}$.

In its turn, $P_1 = 20\text{ Torr}$, and P_2 is the value we need to compute (vapour pressure at 350K).

R is the gas constant, $R = 1.987 \frac{\text{cal}}{\text{K}\cdot\text{mol}}$.

If we assume, that the change in heat capacity for this temperature interval is zero ($\Delta c_p = 0$), sublimation enthalpy ΔH_{subl} is equal at both temperatures. Now, we should rearrange the equation to get $\ln(P_2)$, knowing that $\ln\left(\frac{P_2}{P_1}\right) = \ln(P_2) - \ln(P_1)$:

$$\begin{aligned}\ln(P_2) &= \ln(P_1) + \frac{\Delta H_{\text{subl}}}{R} \left(\frac{1}{T_1} - \frac{1}{T_2}\right) \\ \ln(P_2) &= \ln(20\text{ Torr}) + \frac{8 \cdot 10^3 \frac{\text{cal}}{\text{mol}}}{1.987 \frac{\text{cal}}{\text{K}\cdot\text{mol}}} \left(\frac{1}{300\text{K}} - \frac{1}{350\text{K}}\right) \\ P_2 &= 136\text{ Torr}\end{aligned}$$

Answer: 136 Torr