

Answer on Question #62784, Chemistry / General Chemistry

Problem 6.95

An electron is accelerated through an electric potential to a kinetic energy of 13.4 keV.

1) What is its characteristic wavelength? [Hint: Recall that the kinetic energy of a moving object is $E = \frac{1}{2}mv^2$, where m is the mass of the object and v is the speed of the object.]

Solution:

13.4 KeV = 1.34×10^4 eV, where 1 electron volt = 1.6022×10^{-19} joules

$$E = (1.34 \times 10^4 \text{ eV}) (1.6022 \times 10^{-19} \text{ J}) / (1 \text{ eV}) = 2.15 \times 10^{-15} \text{ J}$$

mass of electron = 9.109×10^{-31} kg

$$v = \text{square root } (2E/m) = \text{sq. root } [2(2.15 \times 10^{-15} \text{ J}) / (9.109 \times 10^{-31} \text{ kg})] = 6.86 \times 10^7 \text{ m/s}$$

$$E = hv/\lambda,$$

Where λ = wavelength and h = Planck's constant

$$\lambda = hv/E = (6.626 \times 10^{-34} \text{ J.s})(6.86 \times 10^7 \text{ m/s}) / (2.15 \times 10^{-15} \text{ J})$$

$$\lambda = 2.12 \times 10^{-11} \text{ m}$$

This is the wavelength of x-rays

Answer: 2.12×10^{-11} m